

# GONIOMETRIE → VZOREC

Hodnoty funkcí pro některé hodnoty  $x$

$x$	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\pi$	$\frac{3\pi}{2}$	$2\pi$
	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$	$180^\circ$	$270^\circ$	$360^\circ$
$\sin x$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	0	-1	0
$\cos x$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	-1	0	1
$\operatorname{tg} x$	0	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$	*	0	*	0
$\operatorname{cotg} x$	*	$\sqrt{3}$	1	$\frac{\sqrt{3}}{3}$	0	*	0	*

$$\rightarrow \operatorname{tg} x = \frac{\sin x}{\cos x}, \quad x \neq \frac{\pi}{2} + k\pi$$

$$\rightarrow \operatorname{cotg} x = \frac{\cos x}{\sin x}, \quad x \neq k\pi, \quad x \neq k \cdot 180^\circ$$

$$\rightarrow \begin{aligned} \sin 2x &= 2 \sin x \cos x \\ \cos 2x &= \cos^2 x - \sin^2 x \end{aligned}$$

Pro každé  $x$ , pro které je funkce definována

$$\begin{aligned} \sin(-x) &= -\sin x \\ \cos(-x) &= \cos x \\ \operatorname{tg}(-x) &= -\operatorname{tg} x \\ \operatorname{cotg}(-x) &= -\operatorname{cotg} x \end{aligned}$$

Pro každé  $x$

$$\begin{aligned} \rightarrow \sin^2 x + \cos^2 x &= 1 \\ \rightarrow \operatorname{tg} x \cdot \operatorname{cotg} x &= 1 \end{aligned}$$

Pro každé  $x$  a  $y$

$$\begin{aligned} \sin(x+y) &= \sin x \cos y + \cos x \sin y \\ \sin(x-y) &= \sin x \cos y - \cos x \sin y \\ \cos(x+y) &= \cos x \cos y - \sin x \sin y \\ \cos(x-y) &= \cos x \cos y + \sin x \sin y \end{aligned}$$

Součet a rozdíl funkcí

Pro každé  $x$  a  $y$

$$\begin{aligned} \sin x + \sin y &= 2 \sin \frac{x+y}{2} \cos \frac{x-y}{2} \\ \sin x - \sin y &= 2 \cos \frac{x+y}{2} \sin \frac{x-y}{2} \\ \cos x + \cos y &= 2 \cos \frac{x+y}{2} \cos \frac{x-y}{2} \\ \cos x - \cos y &= -2 \sin \frac{x+y}{2} \sin \frac{x-y}{2} \end{aligned}$$

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