

Metoda per partes (po částech)

$$\begin{aligned}\int x^2 \cos(3x) dx &= \left| \begin{array}{ll} u' = \cos(3x) & v = x^2 \\ u = \frac{1}{3} \sin(3x) & v' = 2x \end{array} \right| = \frac{1}{3} x^2 \sin(3x) - \frac{2}{3} \int x \sin(3x) dx = \left| \begin{array}{ll} u' = \sin(3x) & v = x \\ u = -\frac{1}{3} \cos(3x) & v' = 1 \end{array} \right| \\ &= \frac{1}{3} x^2 \sin(3x) - \frac{2}{3} \left(-\frac{1}{3} x \cos(3x) + \frac{1}{3} \int \cos(3x) dx \right) = \underline{\underline{\frac{1}{3} x^2 \sin(3x) + \frac{2}{9} x \cos(3x) - \frac{2}{27} \sin(3x) + C}}\end{aligned}$$

$$\int x^2 \cos x dx = \underline{\underline{(x^2 - 2) \sin x + 2x \cos x + C}}$$

$$\int x^2 \sin(2x) dx = \underline{\underline{-\frac{1}{2} x^2 \cos(2x) + \frac{1}{2} x \sin(2x) + \frac{1}{4} \cos(2x) + C}}$$

$$\int x \sin x dx = \underline{\underline{-x \cos x + \sin x + C}}$$

$$\int x \cos(4x + 3) dx = \underline{\underline{\frac{1}{4} \sin(4x + 3) + \frac{1}{16} \cos(4x + 3) + C}}$$

$$\int x^2 \sin \frac{x}{2} dx = \underline{\underline{-2x^2 \cos \frac{x}{2} + 8x \sin \frac{x}{2} + 16 \cos \frac{x}{2} + C}}$$

$$\int x e^{3x} dx = \left| \begin{array}{ll} u' = e^{3x} & v = x \\ u = \frac{1}{3} e^{3x} & v' = 1 \end{array} \right| = \underline{\underline{\frac{1}{3} x e^{3x} - \frac{1}{9} e^{3x} + C}}$$

$$\begin{aligned}\int (x^2 + 1) e^{-x} dx &= \left| \begin{array}{ll} u' = e^{-x} & v = x^2 + 1 \\ u = -e^{-x} & v' = 2x \end{array} \right| = -e^{-x} (x^2 + 1) + 2 \int x e^{-x} dx = \left| \begin{array}{ll} u' = e^{-x} & v = x \\ u = -e^{-x} & v' = 1 \end{array} \right| \\ &= -e^{-x} (x^2 + 1) + 2 \left(-x e^{-x} + \int e^{-x} dx \right) = -e^{-x} (x^2 + 1) - 2x e^{-x} - 2e^{-x} + C \\ &= \underline{\underline{-e^{-x} (x^2 + 2x + 3) + C}}\end{aligned}$$

$$\int x e^{-x} dx = \left| \begin{array}{ll} u' = e^{-x} & v = x \\ u = -e^{-x} & v' = 1 \end{array} \right| = -x e^{-x} + \int e^{-x} dx = \underline{\underline{-x e^{-x} - e^{-x} + C}}$$

$$\int (x^2 - x + 2) e^{3x} dx = \underline{\underline{\frac{e^{3x}}{27} (9x^2 - 15x + 23) + C}}$$

$$\int x e^{-2x} dx = \underline{\underline{-\frac{1}{4} e^{-2x} (2x + 1) + C}}$$

$$\int (x^2 + 2x + 17) e^x dx = \underline{\underline{(x^2 + 17) e^x + C}}$$

$$\int x^2 3^x dx = \underline{\underline{\frac{3^x}{\ln 3} \left(x^2 - \frac{2x}{\ln 3} + \frac{2}{\ln^2 3} \right) + C}}$$

$$\begin{aligned}\int \ln^2 x dx &= \left| \begin{array}{ll} u' = 1 & v = \ln^2 x \\ u = x & v' = 2 \ln x \frac{1}{x} \end{array} \right| = x \ln^2 x - 2 \int \ln x dx = \left| \begin{array}{ll} u' = 1 & v = \ln x \\ u = x & v' = \frac{1}{x} \end{array} \right| \\ &= \underline{\underline{x \ln^2 x - 2x \ln x + 2x + C}}\end{aligned}$$

$$\int x \ln x dx = \left| \begin{array}{ll} u' = x & v = \ln x \\ u = \frac{x^2}{2} & v' = \frac{1}{x} \end{array} \right| = \frac{x^2}{2} \ln x - \int \frac{x}{2} dx = \underline{\underline{\frac{x^2}{2} \ln x - \frac{x^2}{4} + C}}$$

$$\int x^5 \ln x dx = \underline{\underline{\frac{x^6}{36} (6 \ln x - 1) + C}}$$

$$\int x^2 \ln x^3 dx = \underline{\underline{x^3 \ln x - \frac{x^3}{3} + C}}$$

$$\int \ln 5x dx = \underline{\underline{x \ln 5x - x + C}}$$

$$\int \frac{\ln x}{x^2} dx = \underline{\underline{-\frac{1}{x}(\ln x + 1) + C}}$$

$$\int \sqrt{x} \ln x dx = \underline{\underline{\frac{2}{3}\sqrt{x^3}(\ln x - \frac{2}{3}) + C}}$$

$$\int \log x dx = \underline{\underline{x \log x - \frac{x}{\ln 10} + C}}$$

$$\begin{aligned} \int e^x \cos(2x) dx &= \left| \begin{array}{l} u' = e^x \quad v = \cos(2x) \\ u = e^x \quad v' = -2 \sin(2x) \end{array} \right| = e^x \cos(2x) + 2 \int e^x \sin(2x) dx = \\ &= \left| \begin{array}{l} u' = e^x \quad v = \sin(2x) \\ u = e^x \quad v' = 2 \cos(2x) \end{array} \right| = e^x \cos(2x) + 2e^x \sin(2x) - 4 \int e^x \cos(2x) dx \\ &\Rightarrow \int e^x \cos(2x) dx = \underline{\underline{\frac{1}{5}(e^x \cos(2x) + 2e^x \sin(2x)) + C}} \end{aligned}$$

$$\begin{aligned} \int e^x \sin(3x) dx &= \left| \begin{array}{l} u' = e^x \quad v = \sin(3x) \\ u = e^x \quad v' = 3 \cos(3x) \end{array} \right| = e^x \sin(3x) - 3 \int e^x \cos(3x) dx = \\ &= \left| \begin{array}{l} u' = e^x \quad v = \cos(3x) \\ u = e^x \quad v' = -3 \sin(3x) \end{array} \right| = e^x \sin(3x) - 3 \left(e^x \cos(3x) + 3 \int e^x \sin(3x) dx \right) \\ &\Rightarrow \int e^x \sin(3x) dx = \underline{\underline{\frac{1}{10}(e^x \sin(3x) - 3e^x \cos(3x)) + C}} \end{aligned}$$

$$\int e^x \sin x dx = \underline{\underline{\frac{1}{2}e^x(\sin x - \cos x) + C}}$$

$$\int e^{2x} \cos 5x dx = \underline{\underline{\frac{e^2 x}{29}(5 \sin 5x + 2 \cos 5x) + C}}$$

$$\begin{aligned} \int \sin^2 x dx &= \left| \begin{array}{l} u' = 1 \quad v = \sin^2 x \\ u = x \quad v' = 2 \sin x \cos x = \sin(2x) \end{array} \right| = x \sin^2 x - \int x \sin(2x) dx = \left| \begin{array}{l} u' = \sin(2x) \quad v = x \\ u = -\frac{1}{2} \cos(2x) \quad v' = 1 \end{array} \right| \\ &= x \sin^2 x + \frac{1}{2} x \cos(2x) - \frac{1}{2} \int \cos(2x) dx = x \sin^2 x + \frac{1}{2} x \cos(2x) - \frac{1}{4} \sin(2x) + C \\ &= x \sin^2 x + \frac{1}{2} x (\cos^2 x - \sin^2 x) - \frac{1}{2} \sin x \cos x + C = \underline{\underline{\frac{1}{2}(x - \sin x \cos x) + C}} \end{aligned}$$